ECE 250

## Data Structures and Algorithms

QUIZ 4
2006-11-20
The quiz is out of 21 marks.
No questions, no aides.
If you are unsure about a question, write down your assumptions and continue.
This examination has two pages of questions.
If you run out of room, use the reverse of this page.

| Surname, Given Name | Student ID |
| :--- | :--- |

Sign here to indicate that you have read the above instructions.

1. [3] Insert $003,513,424,637,246,155$ into the following into the following initiallyempty hash table by using a hash function which maps an integer to its least-significant digit. Use linear probing if a collision occurs.

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |

2. [3] Insert $003,513,424,637,246,155$ into the following into the following initiallyempty hash table by using a hash function which maps an integer to its least-significant digit. Use double hashing if a collision occurs where the second hash function is the appropriately-modified (as discussed in class) second-least-significant digit.

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

3. [2] In a min heap with $n$ elements, what is the number of nodes which must be searched to find the maximum element of the heap? Write your answer as if you were using C++-style integer division (which truncates any fractional part).
4. [3] Given the min heap

|  | 2 | 3 | 5 | 9 | 8 | 12 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

find the state of the min heap after one dequeue of the minimum element using the algorithm shown in class. Enter your answer into the following table:

5. [2] Given the unsorted array

| 5 | 3 | 6 | 2 | 8 | 1 | 4 | 7 | 9 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

perform one pass through the array as defined by the bubble sort algorithm. Enter your answer in this table:

6. [4] Convert the following unsorted list into a max-heap using the $\mathbf{O}(n)$ heapification process shown in class:

| 7 | 8 | 4 | 2 | 3 | 1 | 5 | 6 | 9 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Enter your answer in this table:

|  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

7. [4] In Project 3, you implemented an expression tree for integers. The expression class had a member variable root which is a pointer to an instance of the expression tree class. The constructor creates an instance of the expression tree class storing the integer 0 .
```
class Expression {
    private:
            ExpressionTree * root;
    public:
            Expression( int = 0) );
            ~Expression();
            void add( int ); // this + n
            void subtract( int ); // this - n
};
```

As with Project 3, implement the functions add and subtract but with the following changes:

1. If you are adding a negative number to this, convert it to a subtraction of the absolute value of the number.
2. If you are subtracting a negative number from this, convert it into a sum of this and the absolute value of the number.
3. Leave the expression tree unchanged if you are adding or subtracting 0 .

The relevant elements of the expression tree class are:

```
Class ExpressionTree {
    public:
        ExpressionTree( int = 0, ExpressionTree * = 0, ExpressionTree * = 0
    );
        ~ExpressionTree();
        static const int PLUS = 0; // You must use these
        static const int MINUS = 1;
        static const int TIMES = 2;
        static const int DIVIDE = 3;
};
void Expression::add( int n ) {
```

\}
void ExpressionTree: :subtract ( int $n$ ) \{

