

Recall that a comparison in any sort is any comparison of magnitude of any two entries in a list and which may or may not result in a swap of two values in a list.

8.5a The following is an implementation of merge sort.

```
template <typename Type>
void merge_sort( Type *array, int n ) {
    merge_sort( array, 0, n - 1 );
}

template <typename Type>
void merge_sort( Type *array, int a, int b ) {
    if ( a >= b ) {
        return;
    }

    int mid = (a + b)/2;

    merge_sort( array, a, mid );
    merge_sort( array, mid + 1, b );
    merge( array, a, mid, b );
}
```

Overloading in C++ is where two functions have the same name but different signatures. What is the purpose of overloading the function `merge_sort`?

8.5b Implement the function `merge` used in the above implementation of merge sort:

```
template <typename Type>
void merge( Type *array, int a, int mid, int b ) {
```

```
}
```

8.5c Rewrite the above function so that if the size of the interval being sorted is less than or equal to the static constant `USE_INSERTION_SORT`, which is set to a positive integer greater than or equal to 1.

8.5d Show the steps in applying merge sort where `USE_INSERTION_SORT` is set to 5.

72	92	79	38	84	76	83	72	15	35	57	29	91	42	48	67
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Show the entries prior to each of the successive merges. The last entry has been created for you.

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15	29	35	38	42	48	57	67	72	72	76	79	83	84	91	92
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8.5e Merge sort requires a temporary array of size $\Theta(n)$. If each time merge is called, a new array is allocated, this could be very expensive. Instead, consider the following implementation:

```
template <typename Type>
void merge_sort( Type *array, int n ) {
    merge_sort( array, 0, n - 1 );
}

template <typename Type>
void merge_sort( Type *array, int a, int b ) {
    if ( a >= b ) {
        return;
    }

    Type *tmp_array = new Type[b - a + 1];

    int mid = (a + b)/2;

    merge_sort_internal( array, tmp_array, a, mid );
    merge_sort_internal( array, tmp_array, mid + 1, b );
    merge( array, tmp_array, a, mid, b );

    delete [] tmp_array;
}

template <typename Type>
void merge_sort_internal( Type *array, Type *tmp_array, int a, int b ) {
    if ( a >= b ) {
        return;
    }

    int mid = (a + b)/2;

    merge_sort_internal( array, tmp_array, a, mid );
    merge_sort_internal( array, tmp_array, mid + 1, b );
    merge( array, tmp_array, a, mid, b );
}
```

Re-implement the merge function so that it uses the entries from 0 to $b - 1 + 1$ in this temporary array to perform the merge and then copy the values back into array.