

## ECE-223, Solution for Assignment #8

Digital Design, M. Mano, 3<sup>rd</sup> Edition, Chapter 7

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7.9) A DRAM chip uses two dimensional address multiplexing. It has 13 common address pins with the row address having 1 bit longer than column address. What is the capacity of the memory?

13+12 = 25 Address lines, => Memory Capacity =  $2^{25}$  words

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7.12) A 12-bit Hamming code word containing 8 bits of data and 4 parity bits is read from memory. What was the original 8-bit data word that was written into memory if the 12-bit word read out is as follows:

- a) 000011101010
- b) 101110000110
- c) 101111110100

a)

$$C_1(1,3,5,7,9,11) = 0,0,1,1,1,1 = 0$$

$$C_2(2,3,6,7,10,11) = 0,0,1,1,0,1 = 1$$

$$C_4(4,5,6,7,12) = 0,1,1,1,0 = 1$$

$$C_8(8,9,10,11,12) = 0,1,0,1,0 = 0$$

$$\Rightarrow C = 0110$$

(Data-bits are 3 5 6 7 9 10 11 12)

Error in bit 6 => Corrected 8-bit data = 0 1 0 1 1 0 1 0

b)

$$C_1(1,3,5,7,9,11) = 1,1,1,0,0,1 = 0$$

$$C_2(2,3,6,7,10,11) = 0,1,0,0,1,1 = 1$$

$$C_4(4,5,6,7,12) = 1,1,0,0,0 = 0$$

$$C_8(8,9,10,11,12) = 0,0,1,1,0 = 0$$

$$\Rightarrow C = 0010 \text{ (Parity bit)}$$

(Data-bits are 3 5 6 7 9 10 11 12)

Error in bit 2 => Corrected 8-bit data = 1 1 0 0 0 1 1 0

c)

$$\Rightarrow C = 0000$$

No Error

8-bit Data = 1 1 1 1 0 1 0 0

7.19) Tabulate the truth table for an  $8 \times 4$  ROM that implements the Boolean functions

$$A(x, y, z) = \sum(1, 2, 4, 6)$$

$$B(x, y, z) = \sum(0, 1, 6, 7)$$

$$C(x, y, z) = \sum(2, 6)$$

$$D(x, y, z) = \sum(1, 2, 3, 5, 7)$$

| Inputs |   |   | Outputs |   |   |   |
|--------|---|---|---------|---|---|---|
| x      | y | z | A       | B | C | D |
| 0      | 0 | 0 | 0       | 1 | 0 | 0 |
| 0      | 0 | 1 | 1       | 1 | 0 | 1 |
| 0      | 1 | 0 | 1       | 0 | 1 | 1 |
| 0      | 1 | 1 | 0       | 0 | 0 | 1 |
| 1      | 0 | 0 | 1       | 0 | 0 | 0 |
| 1      | 0 | 1 | 0       | 0 | 0 | 1 |
| 1      | 1 | 0 | 1       | 1 | 1 | 0 |
| 1      | 1 | 1 | 0       | 1 | 0 | 1 |

7.22) List the PLA programming table for the BCD to excess-3 code convert whose Boolean function are simplified in Fig. 4-3.

From Fig.4-3

$$w = A+BC+BD, w' = A'B' + A'C'D'$$

$$x = B'C + B'D + BC'D', x' = B'C'D' + BC + BD$$

$$y = CD + C'D', y' = C'D + CD'$$

$$z = D', z' = D$$

use w, x', y, z ( 7 terms )

|        | Product term | Inputs |   |   |   | Outputs |   |   |   |
|--------|--------------|--------|---|---|---|---------|---|---|---|
|        |              | A      | B | C | D | w       | x | y | z |
| A      | 1            | 1      | - | - | - | 1       | - | - | - |
| BC     | 2            | -      | 1 | 1 | - | 1       | 1 | - | - |
| BD     | 3            | -      | 1 | - | 1 | 1       | 1 | - | - |
| B'C'D' | 4            | -      | 0 | 0 | 0 | -       | 1 | - | - |
| CD     | 5            | -      | - | 1 | 1 | -       | - | 1 | - |
| C'D'   | 6            | -      | - | 0 | 0 | -       | - | 1 | - |
| D'     | 7            | -      | - | - | 0 | -       | - | - | 1 |
|        |              |        |   |   |   | T       | C | T | T |

7.23) Repeat problem 7.22 using a PAL.

| Product Term | AND Inputs |   |   |   | Outputs                 |
|--------------|------------|---|---|---|-------------------------|
|              | A          | B | C | D |                         |
| 1            | 1          | - | - | - | $w = A + BC + BD$       |
| 2            | -          | 1 | 1 | - |                         |
| 3            | -          | 1 | - | 1 |                         |
| 4            | -          | 0 | 1 | - | $x = B'C + B'D + BC'D'$ |
| 5            | -          | 0 | - | 1 |                         |
| 6            | -          | 1 | 0 | 0 |                         |
| 7            | -          | - | 1 | 1 | $y = CD + C'D'$         |
| 8            | -          | - | 0 | 0 |                         |
| 9            | -          | - | - | - |                         |
| 10           | -          | - | - | 0 | $z = D'$                |
| 11           | -          | - | - | - |                         |
| 12           | -          | - | - | - |                         |

7.24) The following is a truth table of a 3-input, 4-output combinational circuit. Tabulate the PAL programming table for the circuit and mark the fuse map in a PAL diagram similar to the one shown in Fig. 7-17.

$\longleftrightarrow y$   

|                   |    |    |    |    |
|-------------------|----|----|----|----|
| $x \backslash yz$ | 00 | 01 | 11 | 10 |
| 0                 |    | 1  |    | 1  |
| 1                 | 1  |    |    | 1  |

$A = yz' + xz' + x'y'z$

$\longleftrightarrow y$   

|                   |    |    |    |    |
|-------------------|----|----|----|----|
| $x \backslash yz$ | 00 | 01 | 11 | 10 |
| 0                 | 1  | 1  | 1  |    |
| 1                 |    |    | 1  | 1  |

$B = xy + yz + x'y'$

$\longleftrightarrow y$

|                   |    |    |    |    |
|-------------------|----|----|----|----|
| $x \backslash yz$ | 00 | 01 | 11 | 10 |
| 0                 |    | 1  |    | 1  |
| 1                 | 1  |    | 1  | 1  |

$x \updownarrow$

$C = A + xyz$

$\longleftrightarrow y$

|                   |    |    |    |    |
|-------------------|----|----|----|----|
| $x \backslash yz$ | 00 | 01 | 11 | 10 |
| 0                 |    | 1  | 1  | 1  |
| 1                 |    | 1  | 1  |    |

$x \updownarrow$

$D = z + x'y$

| Product Term | AND Inputs |   |   |   | Outputs                 |
|--------------|------------|---|---|---|-------------------------|
|              | x          | y | z | A |                         |
| 1            | -          | 1 | 0 | - | $A = yz' + xz' + x'y'z$ |
| 2            | 1          | - | 0 | - |                         |
| 3            | 0          | 0 | 1 | - |                         |
| 4            | 0          | 0 | - | - | $B = x'y' + xy + yz$    |
| 5            | 1          | 1 | - | - |                         |
| 6            | -          | 1 | 1 | - |                         |
| 7            | -          | - | - | 1 | $C = A + xyz$           |
| 8            | 1          | 1 | 1 | - |                         |
| 9            | -          | - | - | - |                         |
| 10           | -          | - | 1 | - | $D = z + x'y$           |
| 11           | 0          | 1 | - | - |                         |
| 12           | -          | - | - | - |                         |