

**University of Waterloo**  
**Department of Electrical and Computer Engineering**  
**ECE 223 Digital Circuits and Systems**  
**Final Examination**  
**Winter 2001**

Duration 3 hours

Instructor: M. Sachdev  
Full marks 100

Date April 9, 2001

Name ..... Student ID .....									
1	2	3	4	5	6	7	8	9	Total

**Notes**

1. Attempt all problems.
2. If information appears to be missing make a reasonable assumption, state it and proceed.
3. Calculators are not needed and are not allowed.
4. No additional material is allowed.
5. Show all steps

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**Problem 1**

Convert following numbers from one radix to another [8]

(A):  $(175.175)_{10}$  to binary

(B):  $(7562.45)_{10}$  to octal

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**Problem 2**

A logic circuit implements the following Boolean function:

$$F = A'C + AC'D'$$

It is found that the circuit input combination  $A = C = 1$  can never occur. Find a simpler expression for  $F$  using the proper don't care conditions. [8]

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**Problem 3**

Simplify the following Boolean function and implement it with a two level NOR gate circuit. Assume true as well as complement values of input variables are available. [12]

$$F(w,x,y,z) = \sum_m(\mathbf{5, 6, 9, 10})$$

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**Problem 4**

Design a combinational circuit that adds one to a 4 bit binary number,  $A_3A_2A_1A_0$ . For example, if the input of the circuit is  $A_3A_2A_1A_0 = 1101$ , the output is  $1110$ . The circuit should be designed using four half-adders **[12]**

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**Problem 5**

Implement the following Boolean function with a **4x1 multiplexer and external gates**. Connect inputs  $A$  and  $B$  to the select lines. The input requirements for the four data lines will be a function of variables  $C$  and  $D$ . These values are obtained by expressing  $F$  as a function of  $C$  and  $D$  for each of the four cases when  $AB = 00, 01, 10, \text{ and } 11$ . [12]

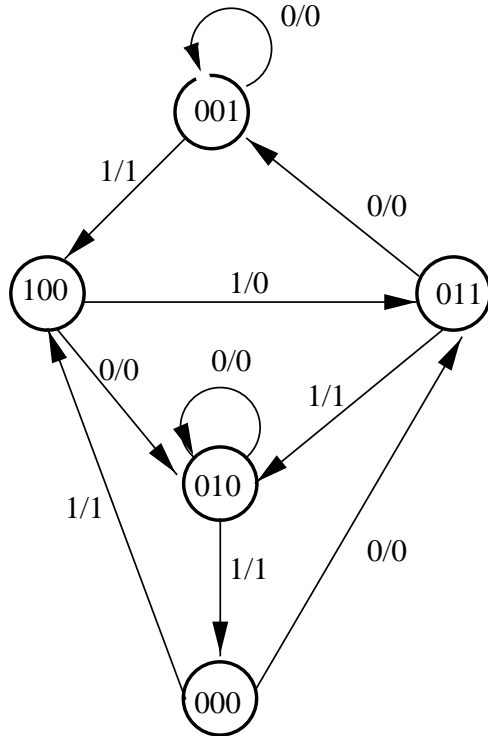
$$F(A,B,C,D) = \Sigma_m(0, 1, 5, 8, 9, 11, 13)$$

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**Problem 6**

A synchronous, sequential circuit has three flip-flops,  $A, B, C$ ; and one input  $x$ ; and one output,  $y$ . The state diagram is shown in the figure. Design the circuit treating the unused states as don't-care conditions. Show the state table and draw the schematic [12]





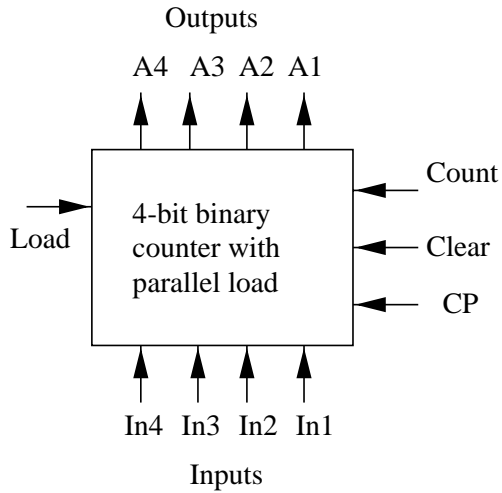


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**Problem 7**

Using two 4-bit binary up counters (one is shown in the figure), construct a binary counter that counts from binary 4 through binary 99. [12]



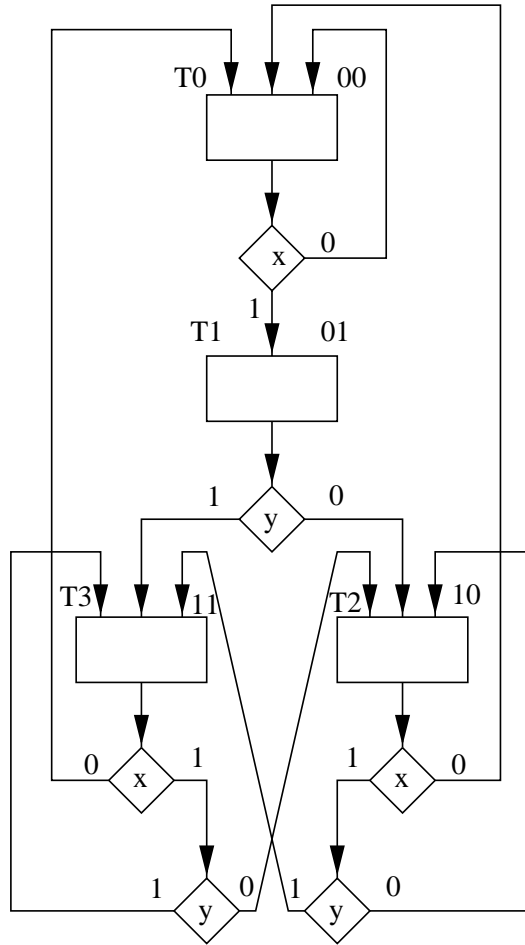
Clear	Clock, CP	Load	Count	Function
0	X	X	X	Clear to 0
1	X	0	0	No change
1	↑	1	X	Load input
1	↑	0	1	Count next binary state

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**Problem 8**

An ASM chart is illustrated in the figure. Construct the state table for the controller. Draw the synchronous, sequential circuit with D flip-flops and combinational logic. [12]



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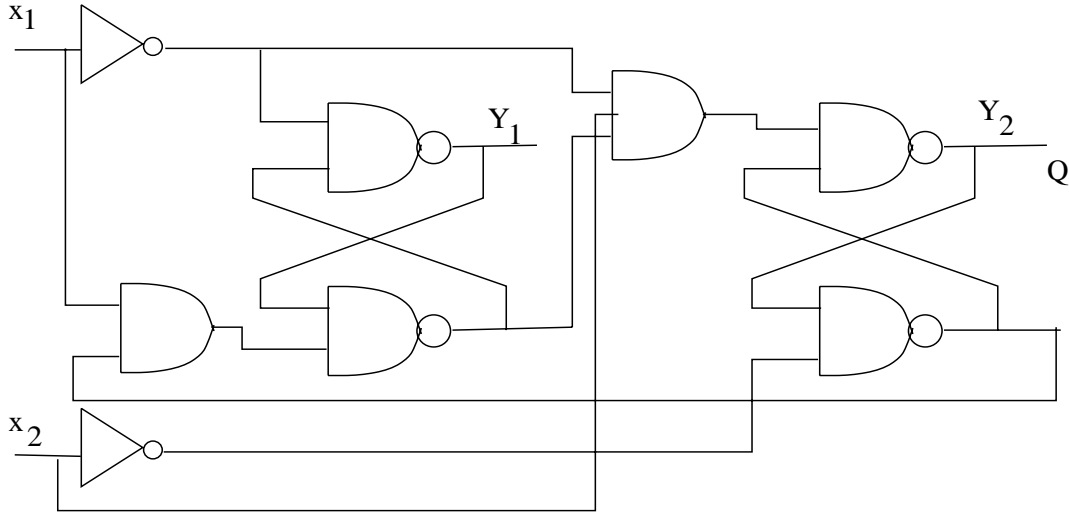
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**Problem 9**

An asynchronous sequential circuit is shown in the figure:

- (i) Derive the Boolean functions for the outputs of the two SR latches  $Y_1$  and  $Y_2$ .
- (ii) Derive the transition table and derive the output map for output  $Q$  of the circuit. [12]



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