### The Computational Sprinting Game

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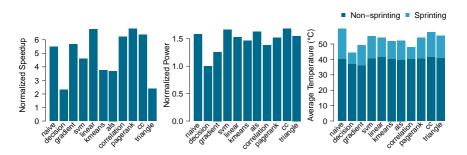
### Computational Sprinting

- Supply extra power to enhance performance for short durations
- Activate more cores, boost voltage/frequency



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### Sprinting Architecture

- Power for sprints supplied by shared rack
- Heat from sprints absorbed by thermal packages

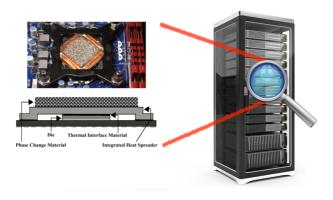
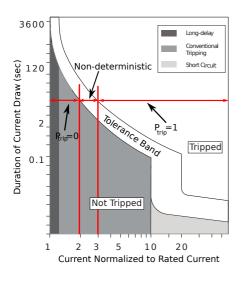




Fig. www.fortlax.se and Raghavan, Arun, et al. "Computational sprinting on a hardware/software testbed."

## Power Emergencies



- Sprints may trip breaker
- Current ↑ with sprinters
- Time ↑ with sprint duration
- Risk ↑ with current, time



Fig. Fu, Wang, and Lefurgy. "How much power oversubscription is safe and allowed in data centers."

### Uninterruptible Power Supplies



- When sprints trip breaker, draw on batteries
- When sprints complete, recharge batteries



### Example – Private Clouds



- Applications compute on servers that share power
- Processors sprint independently
- Processors sprint selfishly for performance



## Sprinting Management

#### When should processors sprint?

- Phases with higher performance from sprints
- But sprints prohibited as chip cools

#### Which processors should sprint?

- Processors that benefit most from sprints
- But sprints prohibited as batteries recover



### Management Desiderata

#### **Individual Performance**

- Sprints account for phase behavior
- Sprints now constrain future sprints

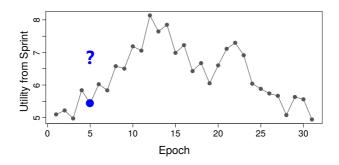
#### **System Stability**

- Sprints account for others' sprinting strategies
- Sprints risk power emergencies



# Sprinting Strategy

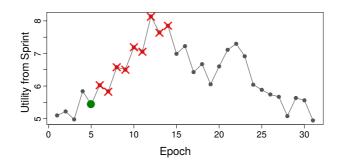
- Optimize sprints given constraints
- Sprint, wait  $\Delta_{cooling}$  for chip cooling
- ullet Sprint, wait  $\Delta_{recovery}$  for rack recovery if breaker trips





# Sprinting Strategy

- Optimize sprints given constraints
- Sprint, wait  $\Delta_{cooling}$  for chip cooling
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### Game Theory

#### Study strategic agents

• Agents selfishly maximize individual utility

#### Optimize responses

• Response maximizes utility, given others' strategies

#### Find equilibrium

State where all agents play their best responses



# Sprinting Game

#### **States**

- Active can sprint
- Cooling cannot sprint, chip cooling
- Recovery cannot sprint, batteries recharging

#### **Actions**

Sprint or not, when active

#### **Strategies**

- Agent's state, app's phase, history, ...
- Others' strategies, utilities, and states, ...



# Mean Field Equilibrium (MFE)

#### **Challenges**

- Large system with many agents
- Complex strategies and many competitors
- Intractable optimization for best response

#### Solution

- Abstract many agents with statistical distributions
- Optimize agents' strategies against expectations



## **Equilibrium Strategy**

#### Agents maximize expected value of (not) sprinting

- Current state
- Utility from sprinting, u
- Probability of tripping,  $P_{trip}$

#### Agents employ threshold strategy

• If active and  $u \ge u_T$ , then sprint

### Find Equilibrium - Offline

ullet Initialize probability of breaker trip  $P_{trip}$ 

- Given  $P_{trip}$ , optimize threshold strategy  $u_T$
- Given  $u_T$ , estimate number of sprinters N
- Given N, update probability  $P'_{trip}$

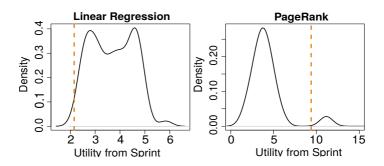
• Iterate if  $P'_{trip} \neq P_{trip}$ 

# Execute Strategy - Online

If active and  $u \geq u_T$ , then sprint



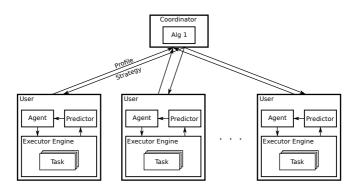
# Sprinting Thresholds



- Thresholds are optimal and diverse
- Agents behave strategically to maximize performance



### Management Architecture



- Offline: coordinator profiles utility, optimizes thresholds
- Online: predictors estimate sprint utility
- Online: agents apply threshold strategy
- Online: executor adapts computation



# **Experimental Methodology**

#### **Sprinting**

• 3 cores  $@1.2\text{GHz} \rightarrow 12 \text{ cores } @2.7\text{GHz}$ 

#### Workloads

- Apache Spark
- Spark engine dynamically schedules tasks on active cores

#### **Performance Metric**

• Tasks completed per second (TPS)

#### Simulation Method

R-based simulator using traces of Spark computation



### Management Policies

#### Greedy

Sprint if neither cooling nor recovering

#### **Exponential Back-off**

- Sprint if neither cooling nor recovering
- Wait randomly for  $U[0, 2^k]$  epochs after  $k^{th}$  trip

#### Cooperative Threshold

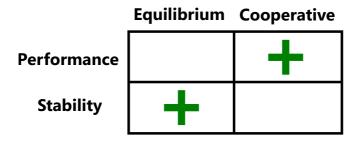
Enforce globally optimized threshold

#### **Equilibrium Threshold**

Announce decentralized, strategic threshold

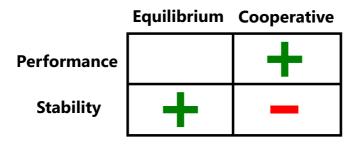


### Case for Equilibria



- Cooperative (+): maximize global performance
- Equilibrium (+): remove incentives to deviate

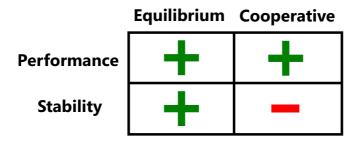
### Case for Equilibria



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- Cooperative (–): enforce strategies globally



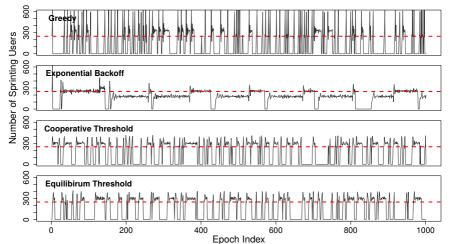
### Case for Equilibria



- Cooperative (+): maximize global performance
- Equilibrium (+): remove incentives to deviate
- Cooperative (–): enforce strategies globally
- Equilibrium (+): maximize individual performance

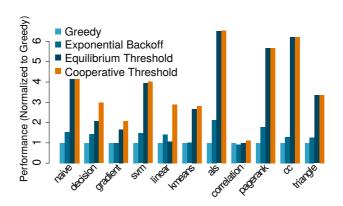


# Sprinting Behavior





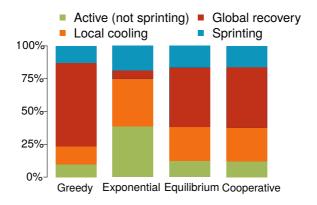
## Sprinting Performance



- Greedy aggressive, incurs emergencies
- Exponential conservative, untimely sprints
- Equilibrium strategic, produces equilibrium
- Cooperative optimal, requires enforcement



#### Game States



- Greedy time in recovery
- Exponential untimely sprints
- Equilibrium timely sprints
- Cooperative timely sprints



#### Conclusion

#### Management with game theory

- Agents sprint according to threshold inexpensive
- Agents have no incentives to deviate stable
- Agents optimize response high performance

#### **Future directions**

- Use game theory to manage scarce resources
- E.g., big/small processors, accelerators

# Thank you

Questions?

